# Circuit Simulation Project 

https://esim.fossee.in/circuit-simulation-project

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Project Name: Design a Full Adder using a 3 X 8 decoder

## THEORY:

A full adder is a digital circuit that performs addition. Full adders are implemented with logical gates in hardware. A full adder adds three one-bit numbers, two operands and a carry bit. The adder outputs two numbers, a sum and a carry bit. The term is contrasted with a half adder, which adds two binary digits.


Full Adder Truth Table:

| Inputs |  |  | Outputs |  |
| :---: | :---: | :---: | :---: | :---: |
| A | B | C-IN | Sum | C-Out |
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |

3 Line to 8 Line Decoder - This decoder circuit gives 8 logic outputs for 3 inputs and has a enable pin. The circuit is designed with AND and NAND logic gates. It takes 3 binary inputs and activates one of the eight outputs. 3 to 8 line decoder circuit is also called as binary to an octal decoder.


A full adder can be implemented with a $3 \times 8$ decoder :


## Equating Full Adder from $3 \times 8$ decoder:

Equation for sum $S=a b{ }^{\prime} c^{\prime}+a^{\prime} b^{\prime} c+a^{\prime} b c^{\prime}+a b c=\Sigma(1,2,4,7)$
Equation for carry out $C=a b+a c+b c$
$=a b\left(c+c^{\prime}\right)+a c\left(b+b^{\prime}\right)+b c\left(a+a^{\prime}\right)$
$=a b c+a b c^{\prime}+a b c+a b^{\prime} c+a b c+a^{\prime} b c$
$=a b c+a^{\prime} b c+a b{ }^{\prime} c+a b c^{\prime}=\Sigma(3,5,6,7)$

From the truth table also we can verify our calculations we can see that:
Sum $=\sum \mathrm{m}(1,2,4,7)$
Carry $=\sum \mathrm{m}(3,5,6,7)$

## Equation for the input and output of Full Adders:

Logical Expression for C-OUT:
$=A^{\prime} B C-I N+A B^{\prime} C-I N+A B C-I N '+A B C-I N$
$=A B+B C-I N+A C-I N$
$=(3,5,6,7)$
Another form in which C-OUT can be implemented:
$=A B+A C-I N+B C-I N\left(A+A^{\prime}\right)$
$=A B C-I N+A B+A C-I N+A^{\prime} B C-I N$
$=A B(1+C-I N)+A C-I N+A^{\prime} B C-I N$
$=A B+A C-I N+A^{\prime} B C-I N$
$=A B+A C-I N\left(B+B^{\prime}\right)+A^{\prime} B C-I N$
$=A B C-I N+A B+A B^{\prime} C-I N+A^{\prime} B C-I N$
$=A B(C-I N+1)+A B^{\prime} C-I N+A^{\prime} B C-I N$
$=A B+A B^{\prime} C-I N+A^{\prime} B C-I N$
$=\mathrm{AB}+\mathrm{C}-\mathrm{IN}\left(\mathrm{A}^{\prime} \mathrm{B}+\mathrm{A} \mathrm{B}^{\prime}\right)$
Therefore COUT $=\mathrm{AB}+\mathrm{C}-\mathrm{IN}(\mathrm{A} E X-O R B)$

## CIRCUIT DIAGRAM:

This` is the main functional circuit schematic for the full adder which uses a 3X8 decoder:


The structure of $3 \times 8$ decoder:


Symbol used for a $3 \times 8$ Decoder:


## OUTPUTS:

## Python Plots:

Inputs:
A



B


C_in


## Outputs:

Sum:


Carry:


Ngspice Plots:
Inputs:
A

Tran1: * c:\users\hp\esim-workspace\adders\adders.cir
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C_in


Outputs:
Sum:


Carry:


## References:

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