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CIRCUIT SIMULATION PROJECT

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Title: Full Subtractor circuit Using Subcircuits (2 Half Subtractors)

THEORY/DESCRIPTION:

In this project, Output Waveforms of Full Subtractor circuit using 2 Half Subtractors in eSim is analysed. A full subtractor is a **combinational circuit** that performs subtraction of two bits, one is minuend and other is subtrahend, taking into account borrow of the previous adjacent lower minuend bit.

This circuit **has three inputs and two outputs**. The three inputs A, B and Bin, denote the minuend, subtrahend, and previous borrow, respectively. The two outputs, D and Bout represent the difference and output borrow, respectively.

Bin is set when the previous digit is borrowed from A. Thus, Bin is also subtracted from A as well as the subtrahend B. Or in symbols: $A - B - Bin$.

Like the half subtractor, the full subtractor generates a borrow out when it needs to borrow from the next digit.

Since we are subtracting B and Bin from A, a borrow out needs to be generated when $A < B + Bin$.

When a borrow out is generated, 2 is added in the current digit. (This is similar to the subtraction algorithm in decimal. Instead of adding 2, we add 10 when we borrow.) Therefore, $D = A - B - Bin + 2Bout$.

TRUTH TABLE:

INPUT			OUTPUT	
A	B	Bin	D	Bout
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

From above table we can draw the K-Map as shown for "Difference" and "Borrow".

		B Bin			
		00	01	11	10
A	0	0	1	0	1
	1	1	0	1	0

$$D = A'B'Bin + AB'Bin' + A'BBin' + ABBin$$

		B Bin			
		00	01	11	10
A	0	0	1	1	1
	1	0	0	1	0

$$Bout = A'Bin + A'B + BBin$$

Logical expression for difference –

$$\begin{aligned}
 D &= A'B'Bin + A'BBin' + AB'Bin' + ABBin \\
 &= Bin (A'B' + AB) + Bin' (AB' + A'B) \\
 &= Bin (A \text{ XNOR } B) + Bin' (A \text{ XOR } B) \\
 &= Bin (A \text{ XOR } B)' + Bin' (A \text{ XOR } B) \\
 &= Bin \text{ XOR } (A \text{ XOR } B)
 \end{aligned}$$

$$= (A \text{ XOR } B) \text{ XOR } \text{Bin}$$

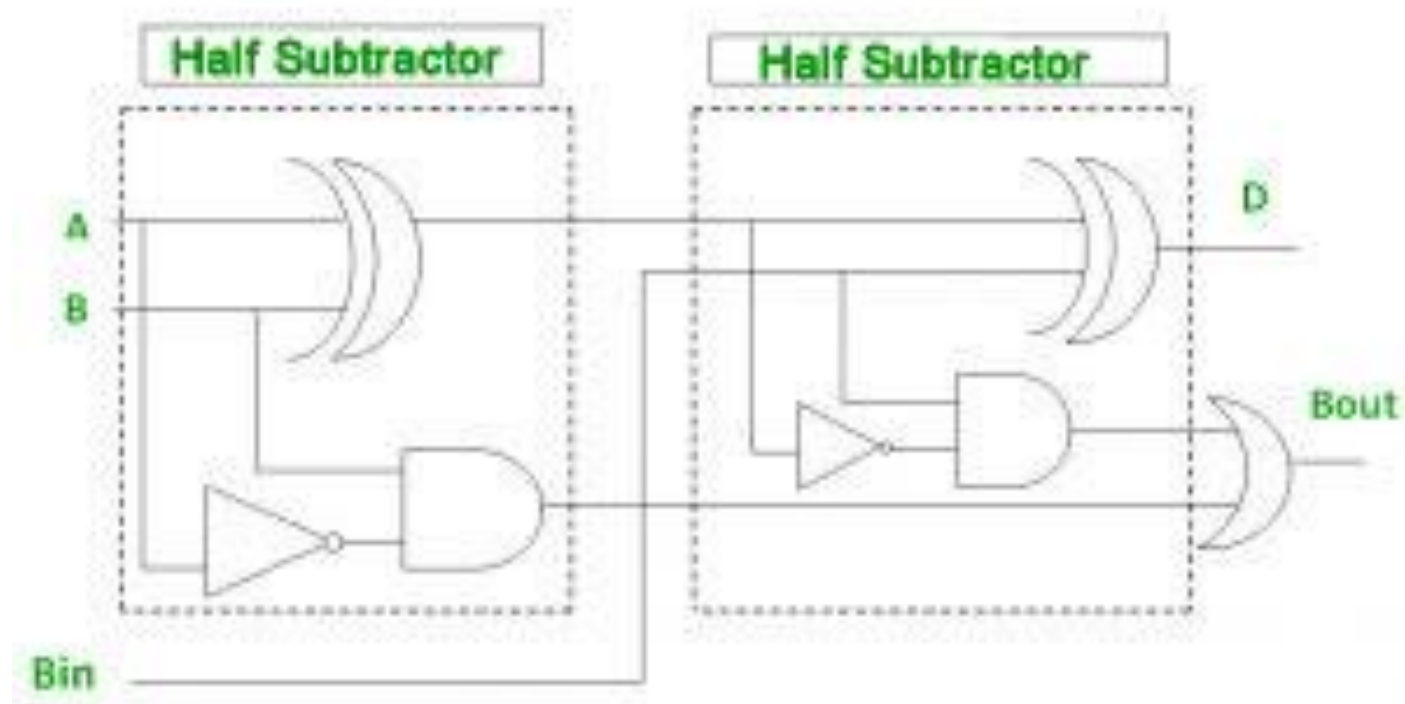
Logical expression for borrow –

$$\begin{aligned} \text{Bout} &= A'B'\text{Bin} + A'BBin' + A'BBin + AB\text{Bin} \\ &= A'B'\text{Bin} + A'BBin' + A'BBin + A'BBin + A'BBin + AB\text{Bin} \\ &= A'\text{Bin}(B + B') + A'B(\text{Bin} + \text{Bin}') + B\text{Bin}(A + A') \\ &= A'\text{Bin} + A'B + B\text{Bin} \end{aligned}$$

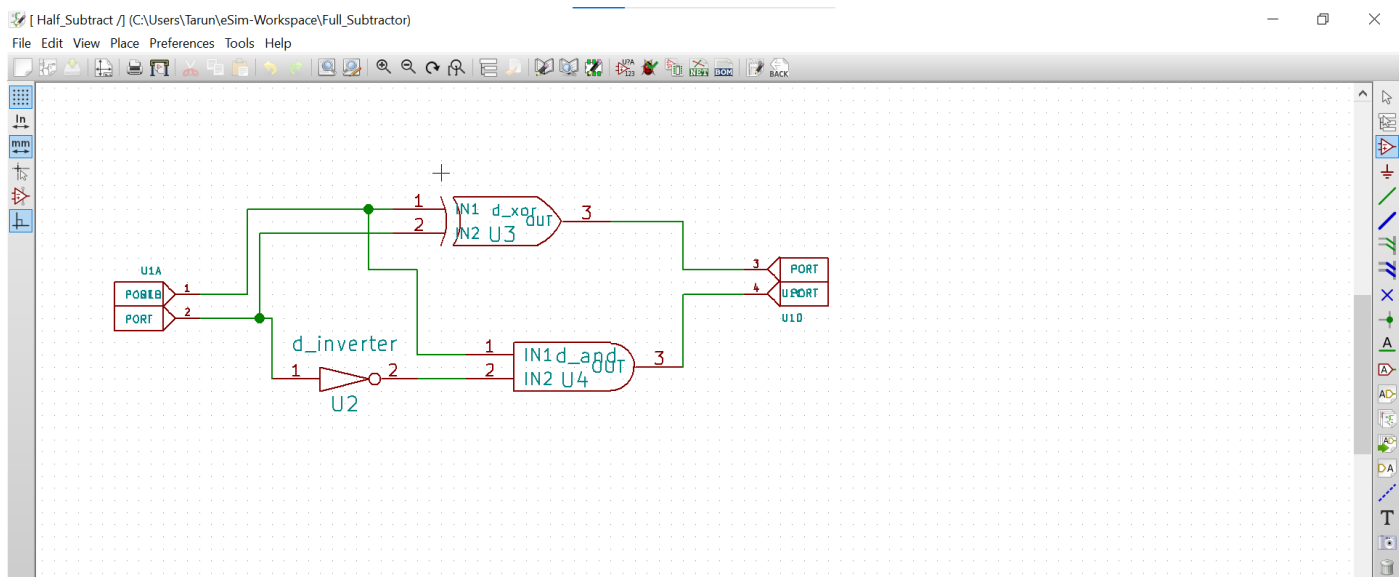
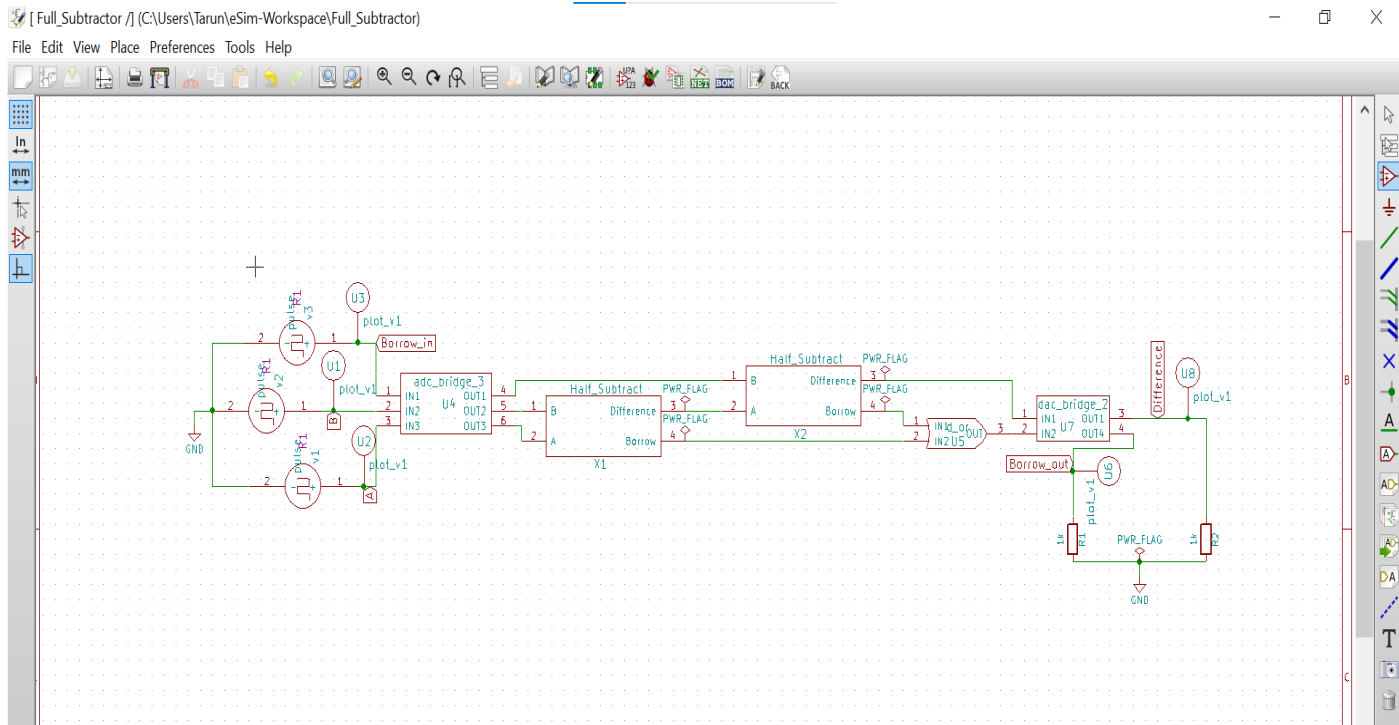
OR

$$\begin{aligned} \text{Bout} &= A'B'\text{Bin} + A'BBin' + A'BBin + AB\text{Bin} \\ &= \text{Bin} (AB + A'B') + A'B (\text{Bin} + \text{Bin}') \\ &= \text{Bin} (A \text{ XNOR } B) + A'B \\ &= \text{Bin} (A \text{ XOR } B)' + A'B \end{aligned}$$

Model Circuit Diagram:

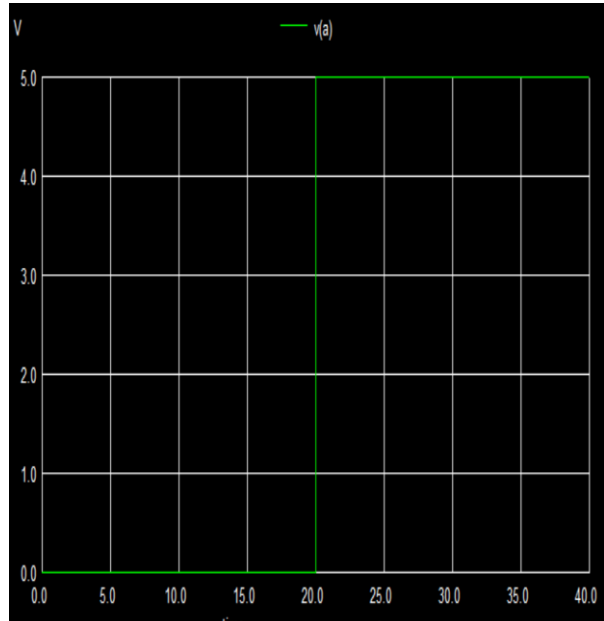
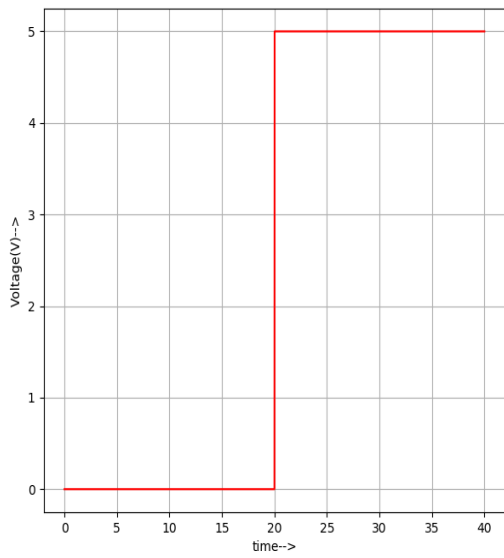


eSim Circuit Diagram:

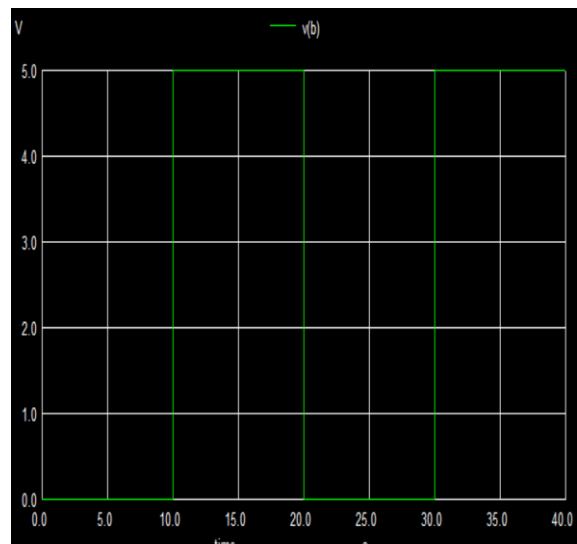
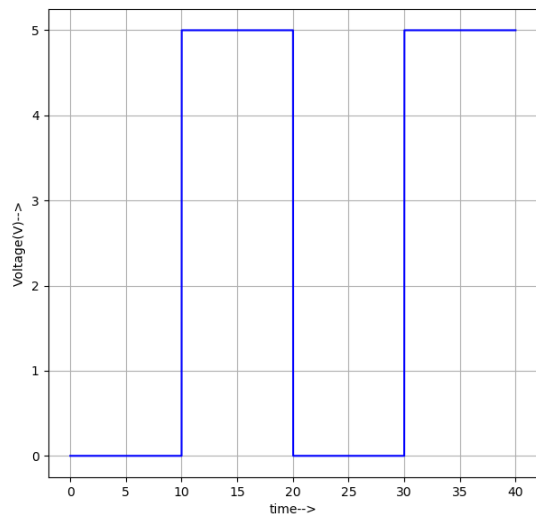


(Half Subtractor SubCircuit)

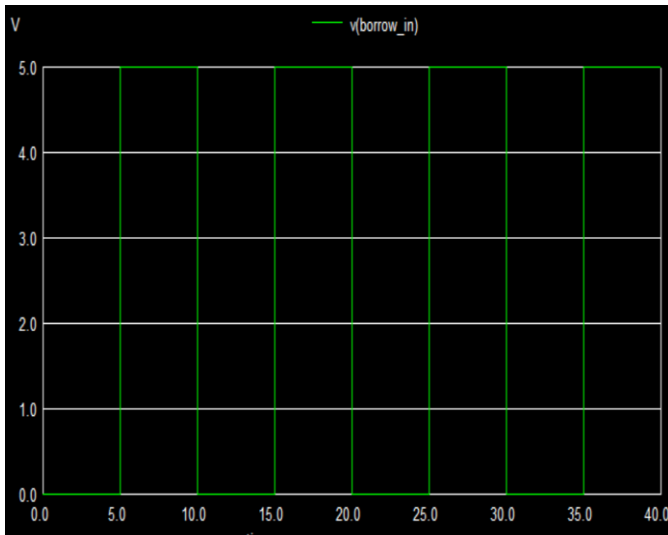
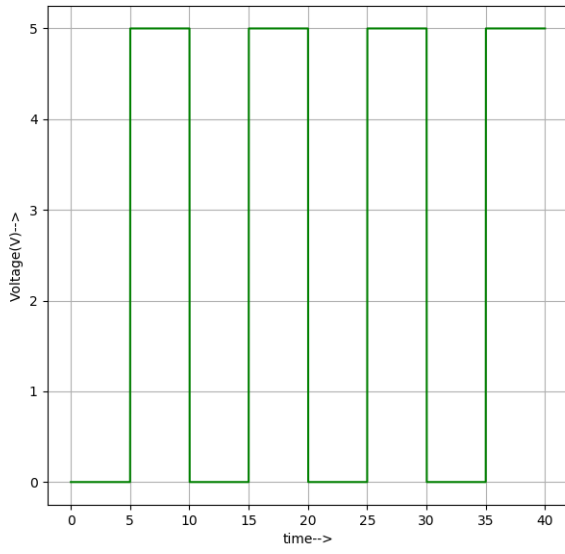
Waveforms (INPUT):



A

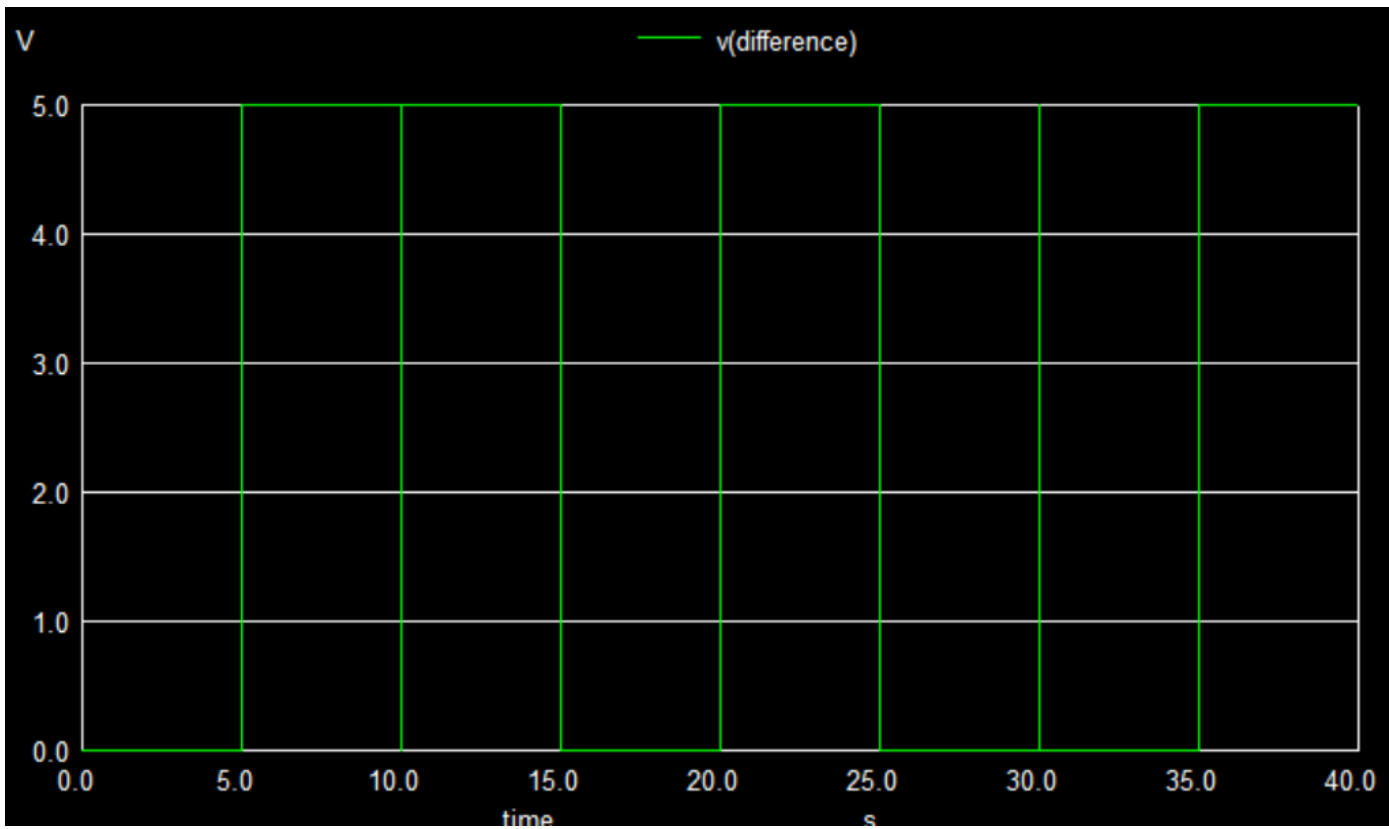
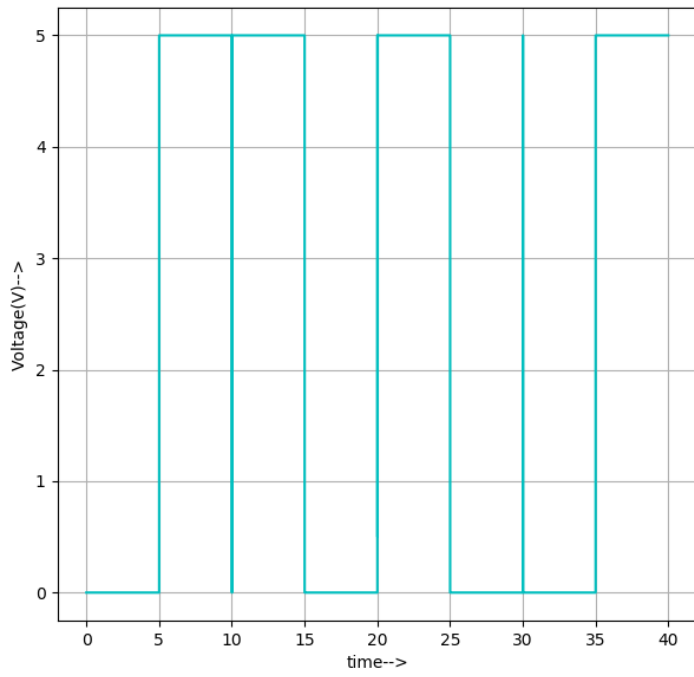


B

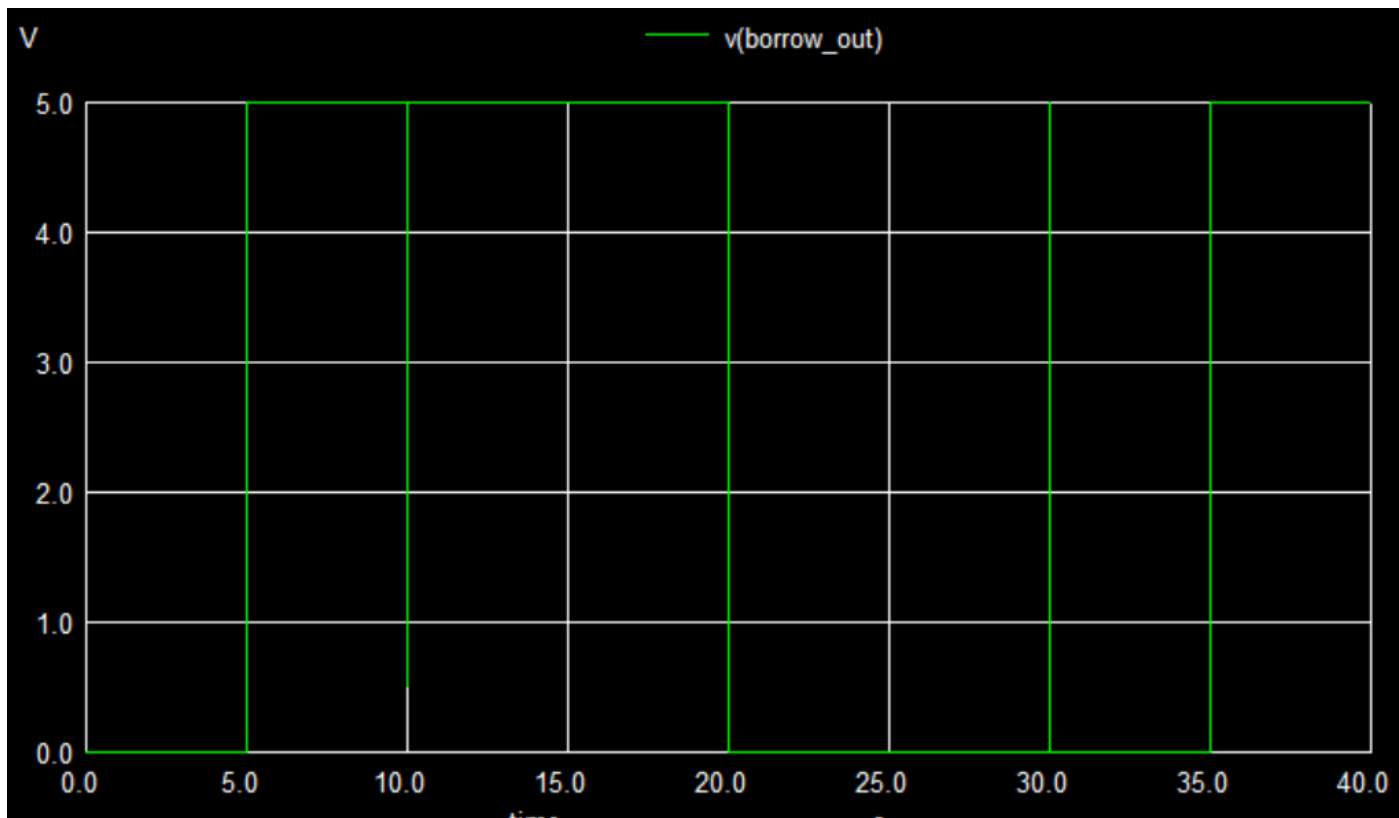
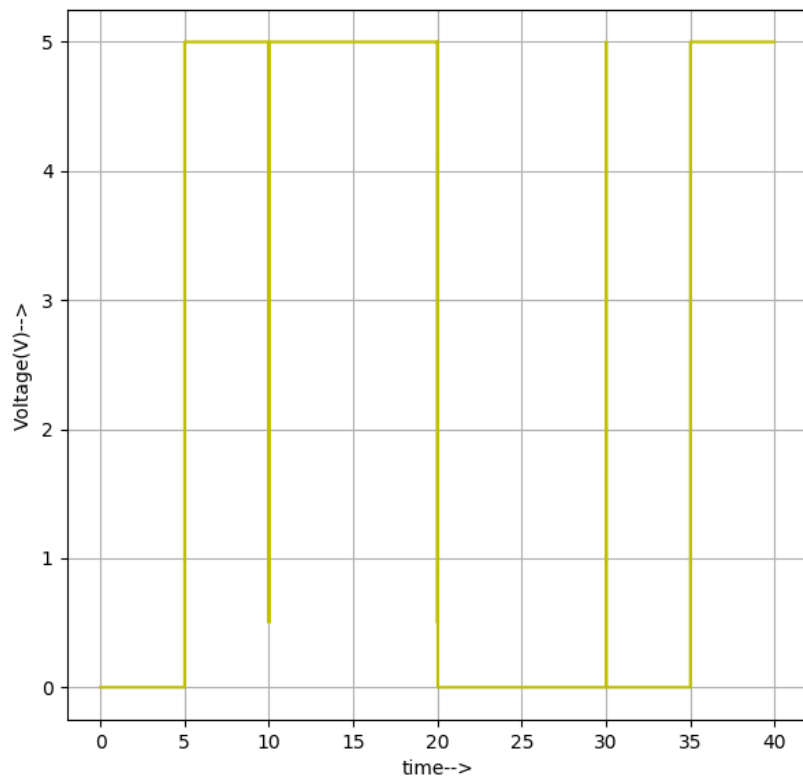


Borrow_in (Bin)

OUTPUT Waveforms:



Difference, D



Borrow_out (Bout)

Conclusion:

Hence, the analysis of Full Subtractor using 2 Half Subtractors in eSim is studied and verified with the waveforms and truth table.

References:

<https://en.wikipedia.org/wiki/Subtractor>

<https://www.geeksforgeeks.org/full-subtractor-in-digital-logic/>